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GUN MUZZLE BLAST FIELD: A COMPUTATIONAL METHOD
BASED ON THE UNIFIED THEORY OF EXPLOSIONS

FINAL REPORT

by

Dennis R. Keefer

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University of Florida
Gainesville, FL

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A computational method of
Henriksen and Cummings based on Porzel's Unified Theory of Explosions has
been extended to permit calculations of the blast field around gun muzzles. The
theory has been extended to permit calculation of the blast field in the region
behind the muzzle exit plane, and uses a different method for the prediction of
overpressure pulse lengths. Predictions based on the theory were compared with
experimentally determined values of overpressure and pulse lengths for guns
from 8 inch diameter to .30 caliber. The theory was found to be adequate for

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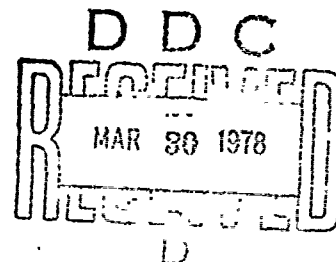
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1. INTRODUCTION

The muzzle blast associated with the firing of a gun can be of sufficient magnitude to cause considerable damage to structures or personnel some distance away from the muzzle. Analytical methods of predicting the characteristics of the blast field are of primary importance to the analysis of a weapon system to insure structural integrity and personnel safety. Ideally, the analytical methods should be based on basic principles so that the blast field can be calculated without resort to empirically determined parameters.

Westine¹ has applied the technique of dimensional analysis to the blast field and, based on the examination of large quantities of experimental data, he presents empirical formulas for the prediction of blast overpressure, pulse length and time-of-arrival. The numerical constants in his equations are given for several barrel elevation angles together with a coefficient which determines the effective energy release for several propellents.

A completely different approach for the prediction of blast fields has recently been devised by Henriksen and Cummings². Their analysis utilizes the Unified Theory of Explosions (UTE) developed by F. B. Porzel³ in the course of an extensive study of nuclear and HE explosions. In their theory Henriksen and Cummings (HC) apply basic principles to evaluate the fraction of propellant energy which is available to the blast field and then use UTE to describe the propagation of the blast with distance. A function was derived to correlate the nonspherical muzzle blast field to the spherical blast field predictions of UTE.

In the present study the basic approach of HC has been retained, but the method of calculating the equivalent hydrodynamics yield has been modified; the non-spherical nature of the gun muzzle blast field has been included in UTE and a completely new method of calculating pulse length has been developed.

-
1. P. S. Westine and J. C. Hokanson, "Prediction of Stand-Off Distances to Present Loss of Hearing from Muzzle Blast", R-CR-75-003 Southwest Research Institute, February, 1975. AD/A-005 274.
 2. B. B. Henriksen and B. E. Cummings, "An a priori Theory for Muzzle Blast Overpressure and Pulse Length Determination", BRL
 3. F. B. Porzel, "Introduction to a Unified Theory of Explosions(UTE)", NOL 72-209, US Naval Ordnance Laboratory, White Oak, Silver Spring, MD, September, 1972. AD 758000.

II. THEORY

A. Porzel's Unified Theory of Explosions

Both HC and the present development depend heavily on the theory and computational methods of Porzel's UTE³. This theory was developed over a period of time and appeared in a number of company and laboratory reports. A fairly comprehensive review of this theory appears in Reference 2 and only a brief synopsis will be presented here.

The UTE is strongly dependent on the separation of the total available energy into "prompt energy" which is available to drive the blast and delayed energy. The prompt energy includes the energy due to static overpressure and dynamic pressure and also includes the kinetic energy due to material velocity. The remaining energy in the explosive is delayed, meaning that it is transported too slowly to support the blast.

This division of energy removes some of the mathematical difficulties associated with the initial instant of energy release and permits an accurate calculation of the prompt energy remaining in the blast wave as it spreads outward and decreases in strength. The basic scaling is encompassed in the QZQ hypothesis which states

$$QZ^q = \text{constant} \quad (1)$$

where Q is the delayed energy (or waste heat), Z is a radial coordinate corrected for the mass of the explosion and q is a constant over a wide range of explosions having the ideal values of 3.5 for strong shocks and 4.0 for weak shocks. If the prompt energy remaining in the blast is known for any blast radius then the entire blast field can be scaled using Equation (1).

The blast overpressure at any radial location can be determined once Q(Z) is known. Porzel³ derives an expression for Q as a function of overpressure based on the Rankine-Hugoniot equations and a generalized equation of state (GES). He also gives a binomial expansion for very low overpressures and an empirical relation for very high overpressures.

The scaling embodied in Equation (1) has been highly successful in predicting the blast field for spherical explosions from one pound of TNT to nuclear explosions. Application of the QZQ hypothesis to gun muzzle blast is complicated by two factors: calculation of the equivalent explosion strength or hydrodynamic yield and the high degree of asymmetry of the blast field compared to a spherical explosion.

B. Equivalent Hydrodynamic Yield for a Gun Muzzle Blast

A central concept in UTE is the division of the explosion energy

into prompt energy which supports the blast wave and delayed energy which does not. The prompt energy includes the energy due to static overpressure and dynamic pressure and also includes the kinetic energy due to material velocity. For a gun the prompt energy available to support the blast is a small fraction of the total propellant energy. A significant fraction of the propellant energy is used to impart kinetic energy to the projectile. Of the remaining energy a significant portion is lost in turbulent boundary layer generation in the gun barrel and impedance of the flow by the tube roughness.

In the previous application of UTE to the muzzle blast problem Henriksen and Cummings have analyzed the barrel loss processes and have shown, based on arguments first advanced by Porzel, that of the remaining energy only one-sixth is prompt energy which can support the blast waves. In their analysis Henriksen and Cummings did not include the kinetic energy of the moving charge in the determination of hydrodynamic yield, but included the directed kinetic energy in their treatment of the non-spherical nature of the blast field.

In the present analysis the kinetic energy of the moving gas at the instant the projectile leaves the barrel is included in the hydrodynamic yield. The initial prompt energy is

$$Y_0 = \frac{1}{6} \{ (M_p \epsilon - KE) \beta + \frac{1}{2} M_p V_m^2 \} \quad (2)$$

where M_p is the propellant mass, ϵ is the specific energy of the propellant, KE is the projectile kinetic energy, β is the barrel loss factor as given by the HC theory and V_m is the muzzle velocity. An initial value of the explosion radius is required in addition to the initial prompt energy in order to use the QZQ hypothesis to predict blast overpressures. For the gun muzzle blast, the initial explosion may be considered as the mass of high pressure gas which exists the muzzle immediately after the projectile has left the muzzle. Schlieren photographs taken at these times show a "barrel shock" system whose characteristic size is of the order of two muzzle diameters. Hence, in the present analysis the barrel diameter is taken as the initial radius. Further, the QZQ scaling is relatively insensitive to the initial radius chosen.

C. The Non-spherical Geometry

Experimental measurements of the blast fields produced by guns have shown that for a fixed distance from the observer to the muzzle, considerably larger overpressures occur in the region forward of the muzzle than in the region behind the muzzle. This is analogous to the moving charge effect which has been studied by Armendt and Sperrazza⁴.

⁴ B. F. Armendt and J. Sperrazza, "Air Blast Measurements Around Moving Explosive Charges, Part III", BRL Memorandum Report No. 1019, U. S. Army Ballistic Research Laboratories Aberdeen Proving Ground, MD, July, 1956.

They found that the blast from a moving charge remained essentially spherical about an origin which moved with the center of mass of the decelerating charge. The deceleration of the charge could be determined by conservation of momentum. The center of mass decelerates rapidly as the expanding shock wave engulfs an ever-growing mass of initially stationary air.

Detailed calculations were made based on this effect and while it predicts higher overpressures forward of the muzzle than aft, the effect is too small to explain the order of magnitude differences which are observed in the muzzle blast experiments. This is due, primarily, to the rapid deceleration of the center of mass which is produced by a rapidly expanding spherical shock.

Porzel³ described a concept called generalized divergence (GDV) which permits an extension of UTE to non-spherical geometries. He notes that the physical significance of the spatial coordinate in the hydrodynamic equations is a radius of curvature rather than the location relative to some earlier position. It is the local radius of curvature of the wave front which determines its divergence. Thus it is the initial shape of the charge which determines the shape of the blast field.

The initial charge for a gun muzzle blast is the barrel gases which exit when the projectile leaves the muzzle. The high overpressure of these gases causes a "barrel shock" system to form as shown schematically in Figure 1. This provides an initial source for the blast field which is far from spherical. The local radius of curvature is much greater in the forward portion of the shock system resulting in a smaller divergence and less rapid decrease in the blast overpressure forward of the gun muzzle compared to the rear where the radius of curvature is much smaller.

The concept of GDV was incorporated into the scaling of blast overpressure provided by the QZQ hypothesis by modifying the distance scale at each angular position in the blast field to correct for the initial non-spherical geometry. The value of R used in the QZQ calculation was given by

$$R = R(\theta)/G(\theta) \quad (3)$$

where $G(\theta)$ is a geometry factor which was determined on an *ad hoc* basis. It was found that the experimental data were reasonably well represented using a geometry factor given by

$$G(\theta) = \frac{3}{4}[\cos \theta + \sqrt{\cos^2 \theta + (4/3)^2}] \quad (4)$$

The derivation of this function was based on a velocity argument and is given in Appendix A.

To summarize, the calculation of overpressure for gun muzzle blast was accomplished by the following sequence:

1. Calculate the initial hydrodynamic yield using Equation (2).
2. The hydrodynamic yield was used to determine the constant in the scaling law, Equation (1).
3. At a given position (distance and angle) in the blast field the value of Q was computed from Equation (1) using a value of R determined from Equations (3) and (4).
4. The blast overpressure at the given field position was determined from the value of Q determined in step 3 using the relations given by Porzel³.

D. Pulse Length Calculations

Henriksen and Cummings² determined the pulse length of the overpressure pulse based on a characteristic length and the particle velocity. The characteristic length was representative of the volume occupied by the remaining prompt energy in the blast.

An alternate method of calculating the pulse length has been developed based on the propagation of waves of finite amplitude. As the blast wave from the explosion expands, the initial high overpressure at the shock front decreases behind the shock front. At some point in the expansion, designated the transition radius, the overpressure behind the shock drops to zero and upon further expansion the blast wave develops a negative phase⁵. The fluid velocity behind the shock has a similar behavior with a large velocity in the direction of the shock velocity decreasing to zero and becoming negative. The resulting pulse forms are shown in Figure 2. These pulses of finite amplitude propagate into the undisturbed air. The propagation velocity is not the same for all portions of the pulse, but depends on the local speed of sound and the fluid velocity. The leading edge of the pulse propagates with a greater velocity than the rest of the pulse and therefore the pulse increases in length as it propagates outward.

The local wave speed for the pulse of finite amplitude is given by⁶

$$c = a_n + u \quad (5)$$

where a_n and u are the local value of the speed of sound and fluid velocity. For an isentropic process the local wave speed becomes

$$c = a + \frac{\gamma+1}{2} u \quad (6)$$

where a is the speed of sound in the undisturbed region ahead of the

5. Yu.B. Zel'dovich and Yu. P. Raizer, Physics of Shock Waves and High-Temperature Hydrodynamic Phenomena, Vol. 1 Academic Press, New York, 1966.
6. H. W. Liepmann and A. Roshko, Elements of Gasdynamics, John Wiley and Sons, New York, 1957.

pulse. The propagation of a shock is not an isentropic process, but for overpressures at distances greater than the transition radius the corrections are small compared to the uncertainty in the measured values.

The trajectories of the pulse front and the point at which the fluid velocity drops to zero are shown in Figure 3. The pulse shape is shown at the transition radius r_0 and at two other positions.

We will define the pulse length τ as the time between these two trajectories at a given position r . Note that as the shock wave expands and the fluid velocity behind the shock approaches zero, the shock front approaches the speed of sound and the pulse length approaches an asymptotic value which then propagates as an acoustic wave.

The zero-velocity trajectory is given by

$$t_1 = \frac{1}{a}(r - r_0) + t_0 + \tau_0 \quad (7)$$

and the shock front velocity by

$$t_2 = \frac{1}{a} \int_{r_0}^r \frac{dx}{1 + \frac{\gamma+1}{2} \frac{u}{a}} + t_0 \quad (8)$$

The difference of these expressions gives the pulse length

$$\tau = \tau_0 + \frac{1}{a} \left[(r - r_0) - \int_{r_0}^r \frac{1}{1 + \frac{\gamma+1}{2} \frac{u}{a}} dx \right] \quad (9)$$

where τ_0 is the initial pulse length at the transition radius r_0 . The initial pulse length τ_0 can be estimated with the aid of Figure 4 which shows the overpressure at the time t when the shock reaches the transition radius⁷. This is the radius for which the negative phase has fully developed and occurs at a pressure ratio of two across the shock. If we make the *ad hoc* assumption that the pulse occupies half the spherical radius at transition then the characteristic initial pulse length is given by

$$\tau_0 = \frac{r_0}{2c_s} \quad (10)$$

where c_s is the wave speed of the shock at a pressure ratio of two.

The pulse length is calculated from Equation (9) using the initial pulse length given in Equation (10) and the fluid velocity determined

7. H. L. Brode, "Numerical Solutions of Spherical Blast Waves", *J. Appl. Phys.*, Vol. 26, No. 6, June 1955, pp. 766-775.

from the Rankine-Hugoniot relations⁷ and the local value of overpressure determined from UTE.

III. RESULTS

The purpose of this study was to determine the applicability of the Henriksen and Cummings theory for smaller caliber guns and to extend the analysis to include those positions aft of the muzzle exit plane. The theory has been applied to predict muzzle blast overpressure for guns ranging from an 8 inch diameter naval gun to a .30 caliber pistol. The predictions of the theory have been compared to the data of Westine⁸ and the results are presented in Figures 5 through 9.

The theory is clearly capable of predicting the muzzle blast overpressure for guns of vastly different calibers. Careful examination of the curves shows that the theory will also predict the angular variations in the blast field with reasonable accuracy over the full range of calibers examined. The largest discrepancy between theory and experiment occurs at distances beyond 50 calibers where the experimental data exceeds the theoretical predictions. The experimental data were all obtained with the guns firing essentially horizontally over the ground or a ground plane. The shock wave associated with the muzzle blast will reflect from this plane causing a reinforcement to the primary shock which increases the measured overpressure. Indeed, in much of the data the measured overpressure values increase with increasing distance from the muzzle for distances beyond 50 calibers. Since the theory does not account for reflected shocks the disagreement at large distances is not surprising.

Examination of the angular behavior of the theory for distances less than 50 calibers for the cases considered reveals that on the average the theoretical predictions tend to overestimate the overpressure in the aft (greater than 90°) portion of the blast field and underestimate the overpressure in the forward portion of the field. This is particularly noticeable for the .30 caliber pistol, the smallest gun considered. This effect is a result of the particular form of the geometry factor chosen. An improvement might be obtained by modifying the form of the geometry factor according to the ratio of random to ordered motion in the muzzle gases as proposed in Reference 2.

Since the current theory contains the kinetic energy of the muzzle gas in the prompt energy the overpressure was calculated for a 105 mm gun in which the muzzle velocity varied as a result of different propellant charges. The results are shown in Figure 10. The theory

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8. P. S. Westine, "Modeling the Blast Field Around Naval Guns and Conceptual Design of a Model Gun Blast Facility," TR 02-2643-01 Southwest Research Institute, September, 1970, AD 875 984.

accurately predicts muzzle blast overpressure for these cases although the muzzle velocity is higher by a factor of two for the zone 8 (Z8) compared to the zone 5 (Z5) experiment. The result shows that the theory will predict the muzzle blast from guns over a considerable range of muzzle velocity.

Pulse length of the overpressure pulse is more difficult to compare since there are large variations in the experimental values obtained. A typical situation is shown in Figure 11 for the case of the same 20 mm gun shown in Figure 7. The theory predicts that the pulse length will increase with distance from the muzzle until it reaches some asymptotic value but the experiments often show that the pulse length first increases then decreases with distance. This decrease first appears at distances greater than 50 calibers and may be related to the shock reflection from the ground plane which produces pulses of complex shapes.

Predicted pulse lengths for four guns ranging from an 8 inch naval gun to a .50 caliber rifle are shown in Figure 12. The pulse length was calculated for an angle of 90° to the line of fire and the experimental data were taken at 75° and 105° . The measured values of pulse length are reasonably well predicted by the theory over the wide range of pulse lengths produced by guns of greatly different caliber.

These results indicate that the current theory gives reasonable agreement with experiment over a wide range of gun calibers. The theory has the advantage of simplicity and ease of calculation and should be of great value in the prediction of free-field gun muzzle blast effects.

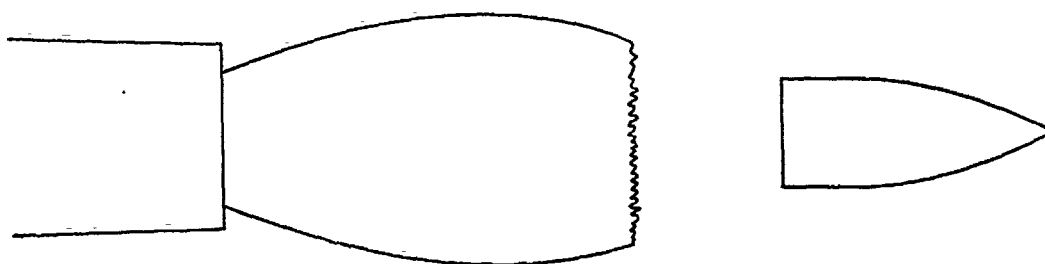


FIGURE 1. "Barrel Shock" Produced by Propellant Gases Exiting Muzzle.

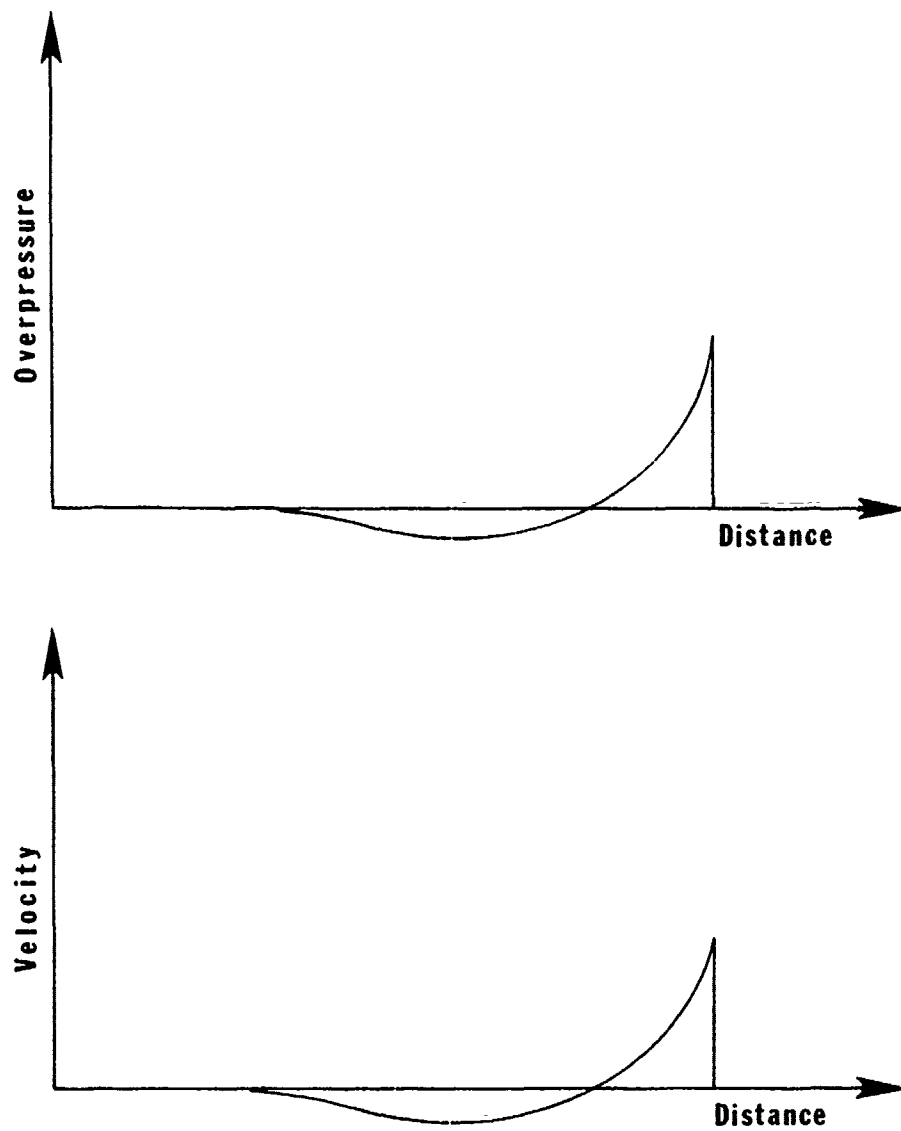


FIGURE 2. Sketch of Overpressure and Fluid Velocity in the Blast Pulse After the Negative Phase Has Developed.

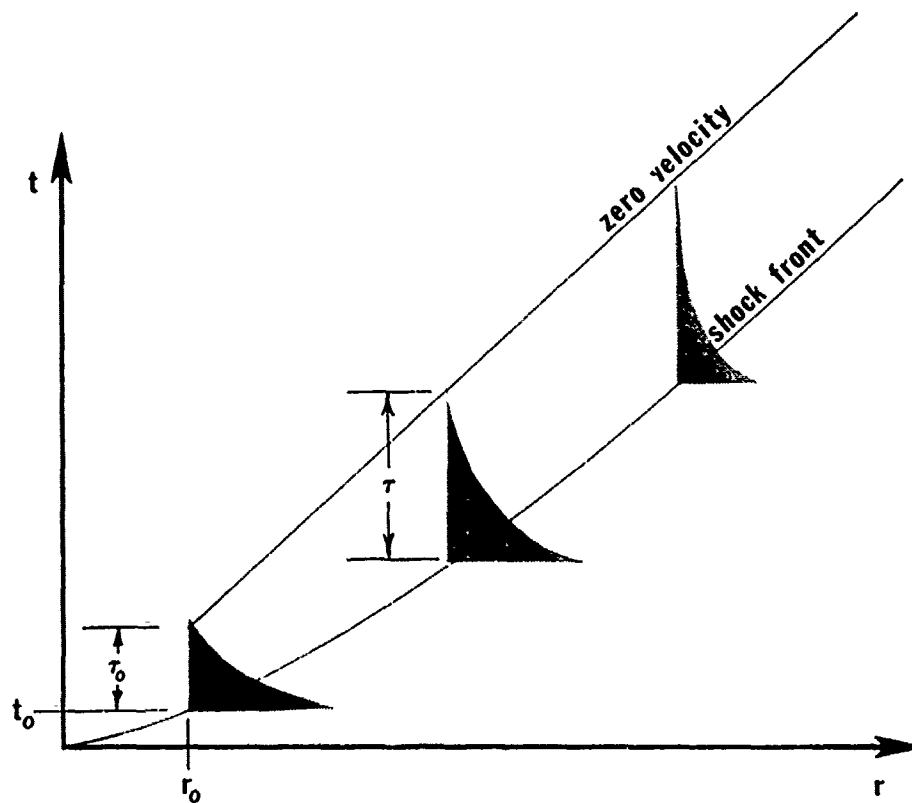


FIGURE 3. Sketch of the Trajectories of the Pulse Front and the Point Where Fluid Velocity Drops to Zero.

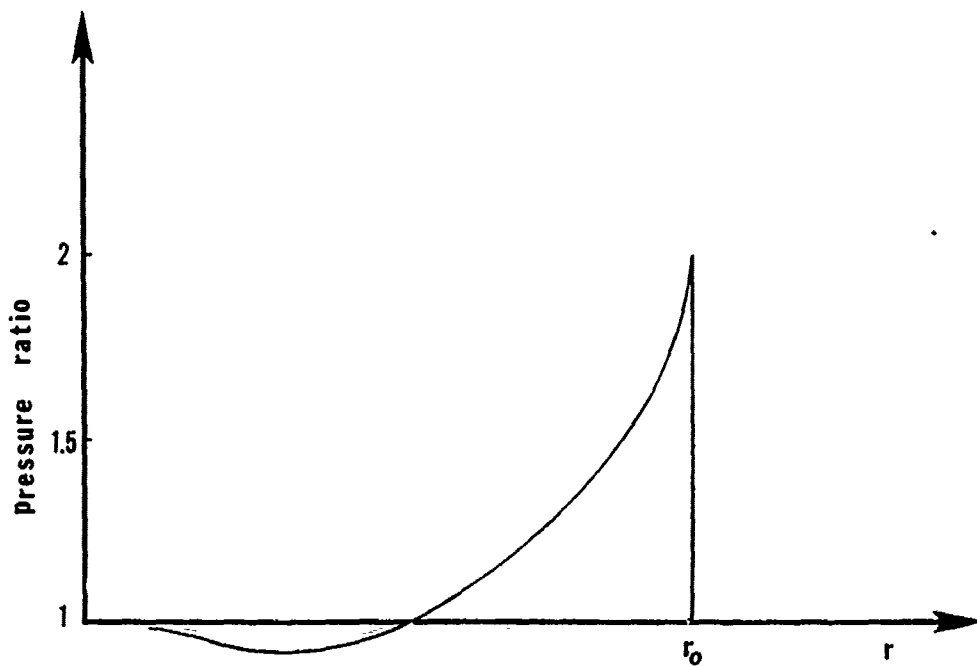


FIGURE 4. Overpressure Pulse at Transition. The Pressure Ratio Drops to Unity of Approximately One-Half the Transition Radius r_0 .

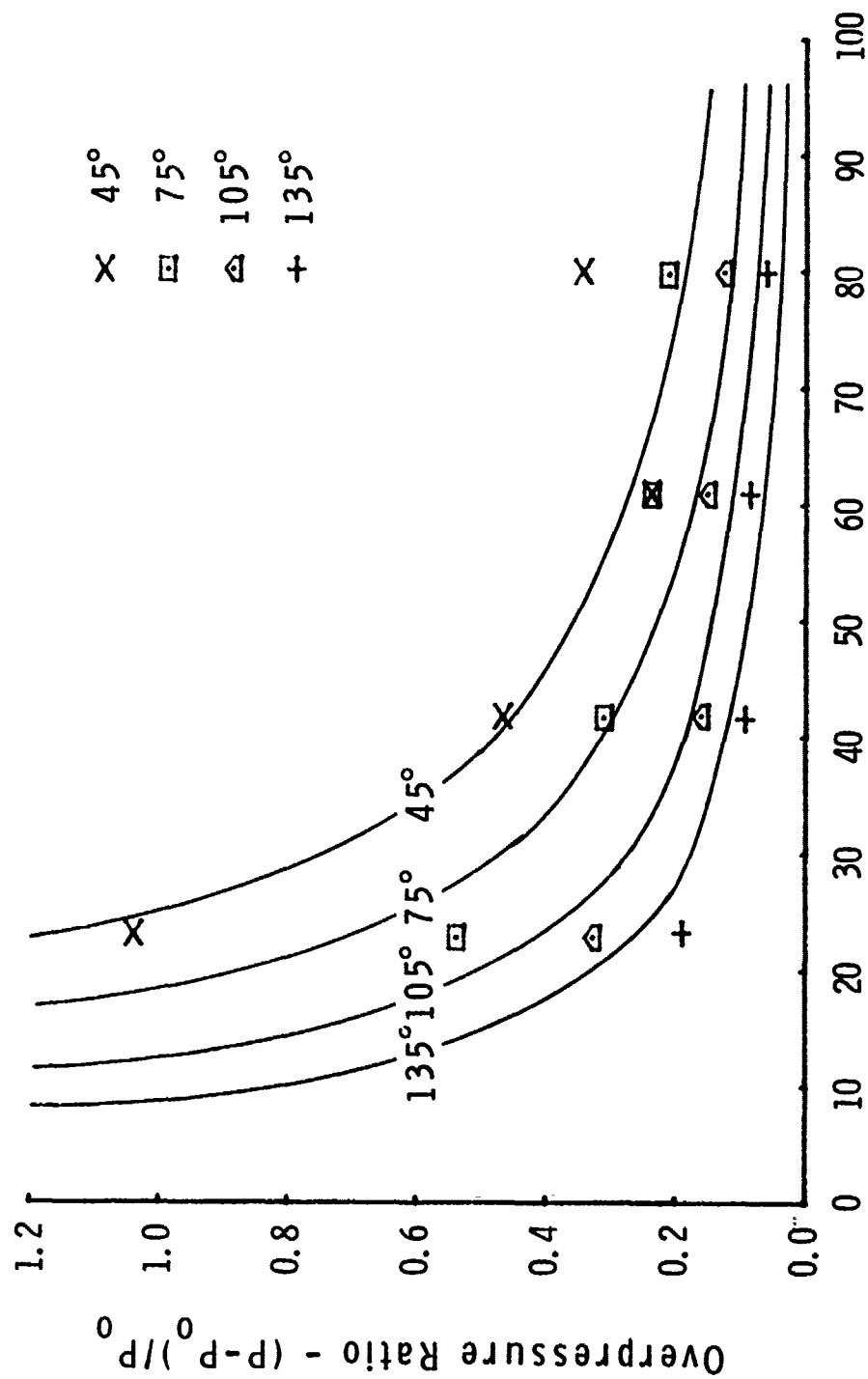


FIGURE 5. Overpressure from 8 inch Naval Gun.

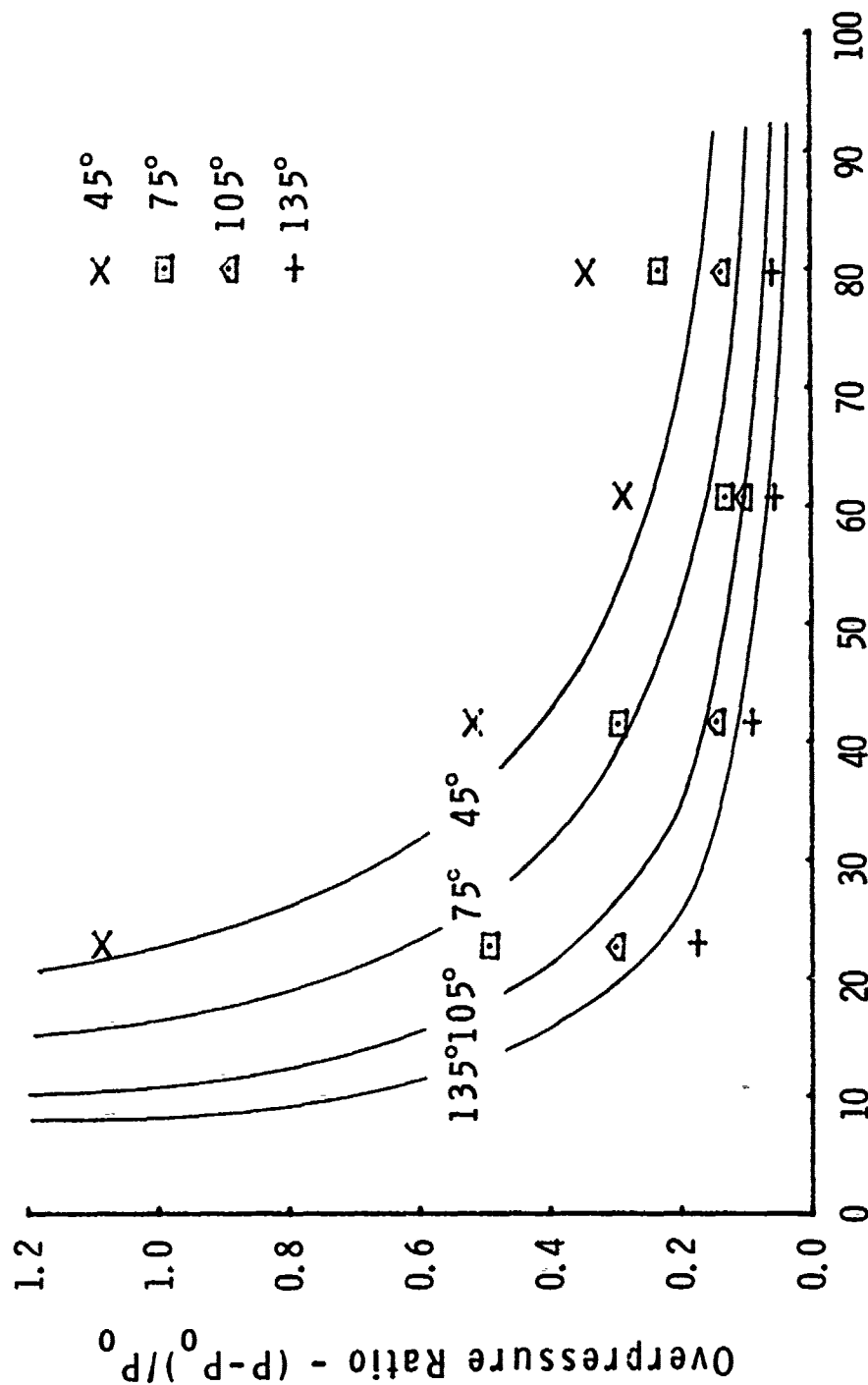
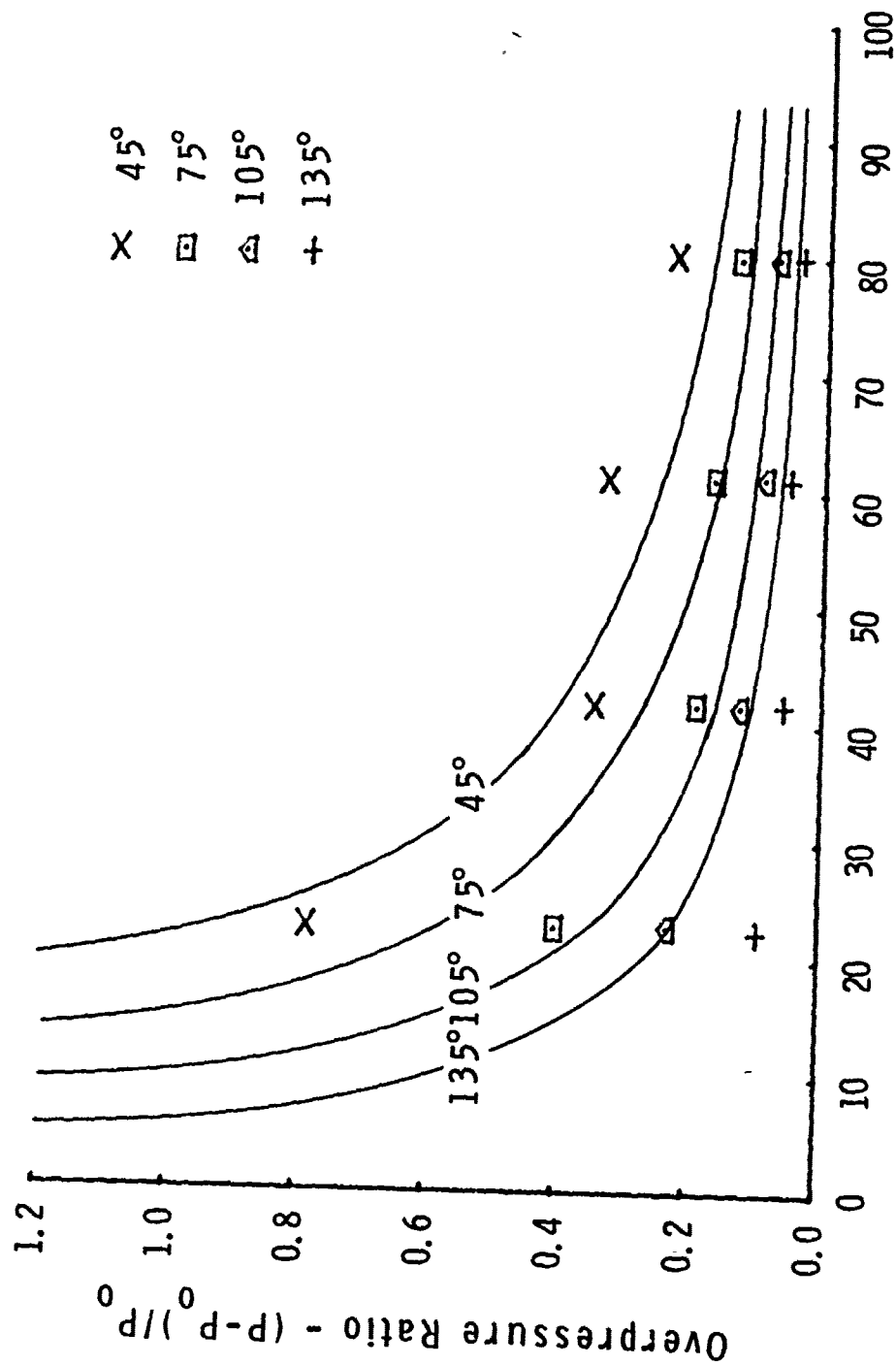
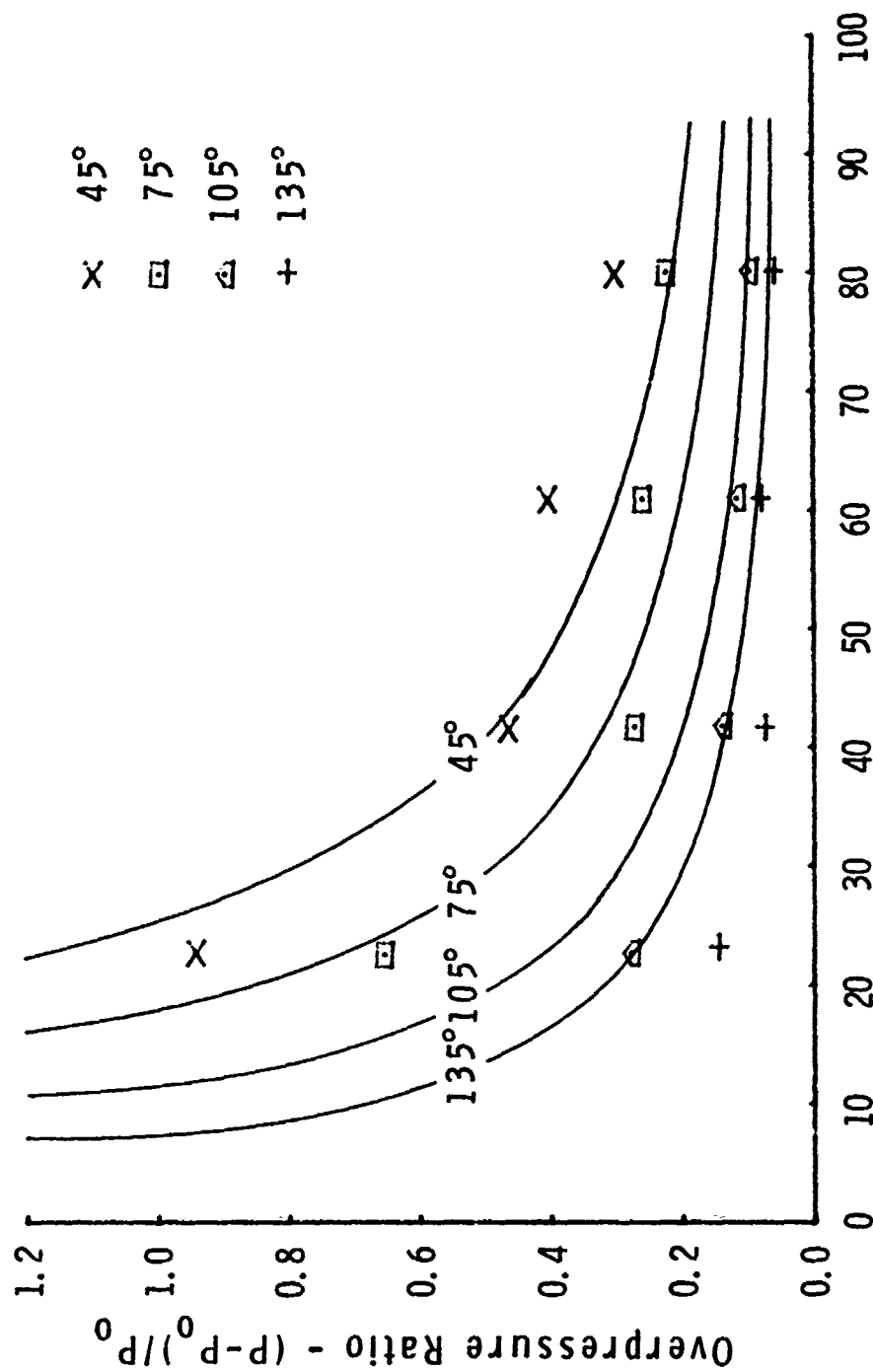


FIGURE 6. Overpressure from 3 inch Naval Gun.



Radial Distance From Muzzle - Calibers

FIGURE 7. Overpressure from 20 mm Gun.



Radial Distance From Muzzle - Calibers

FIGURE 8. Overpressure from .30 Caliber Rifle.

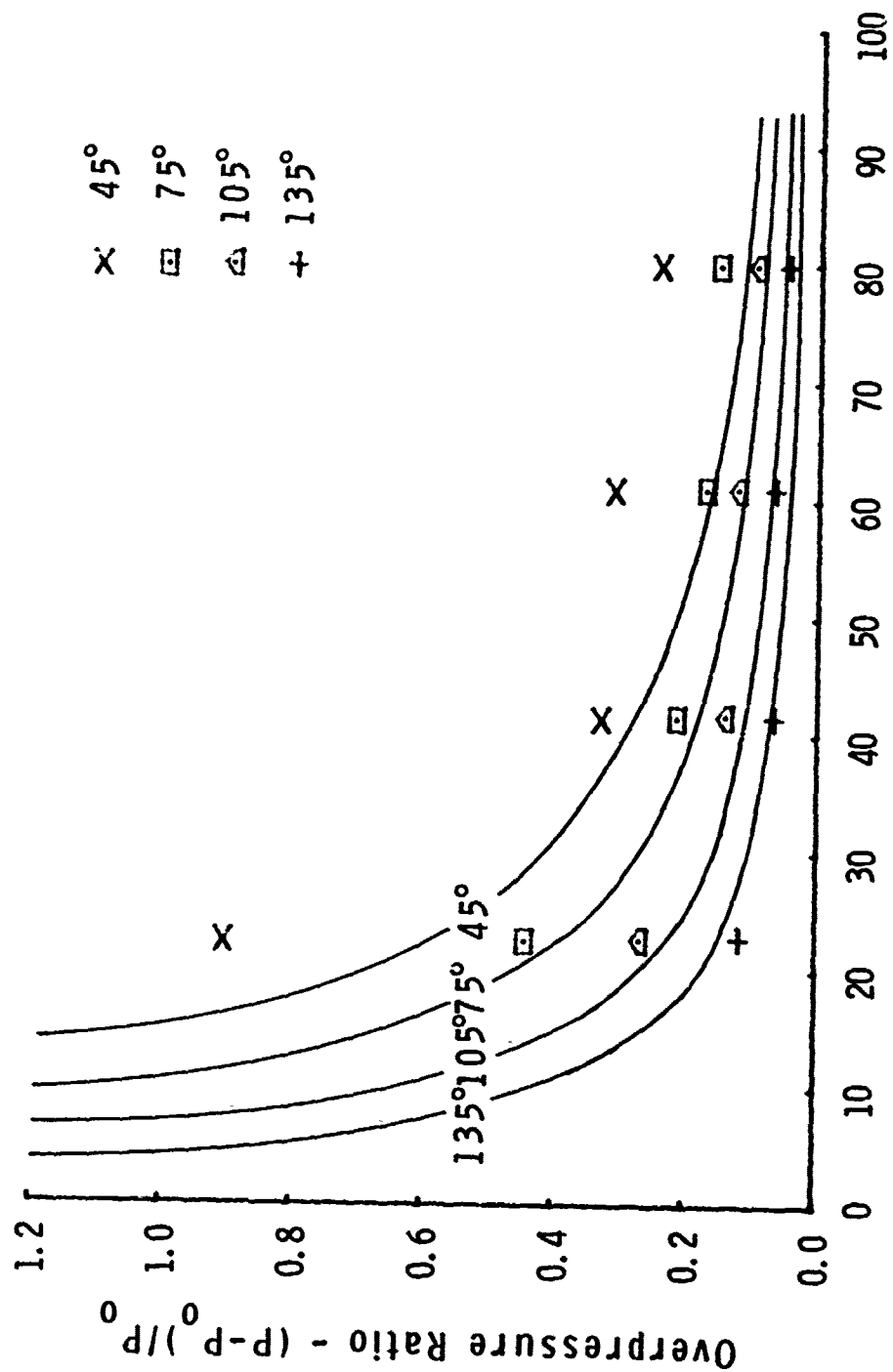


FIGURE 9. Overpressure from .50 Caliber Pistol.

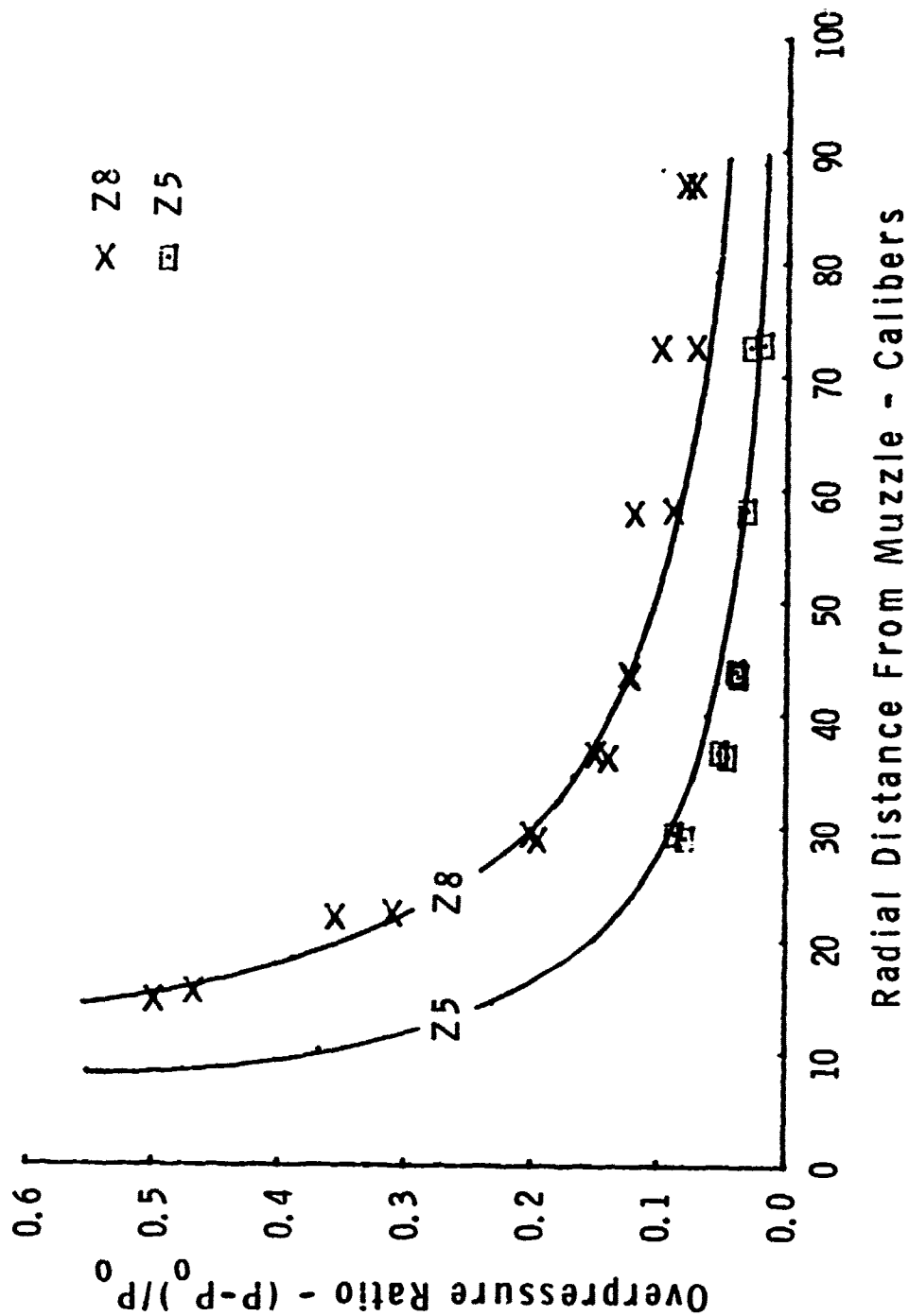
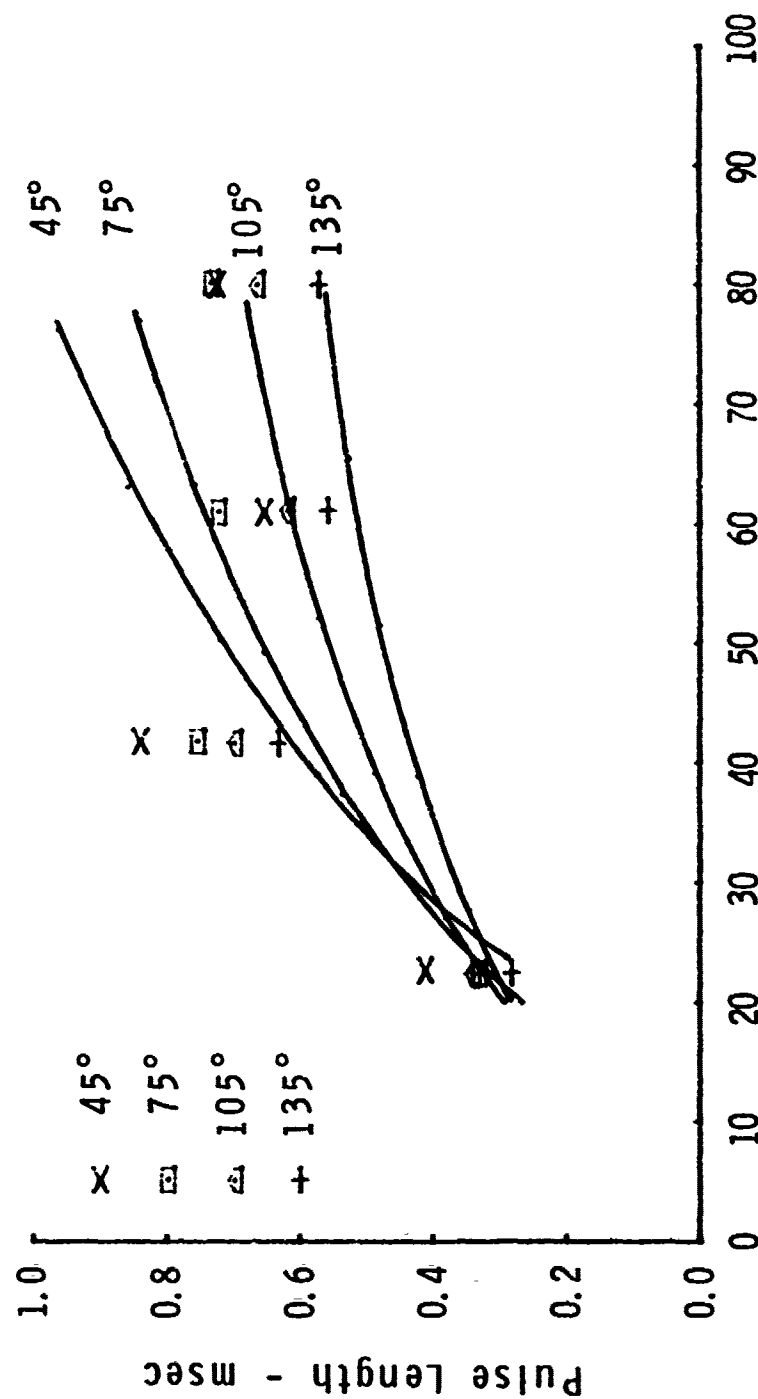


FIGURE 10. Overpressure from 105 mm Howitzer at Two Muzzle Velocities. Z8 is 650 m/s and Z5 is 332 m/s.



Radial Distance From Muzzle - Calibers

FIGURE 11. Overpressure Pulse Length from 20 mm Gun.

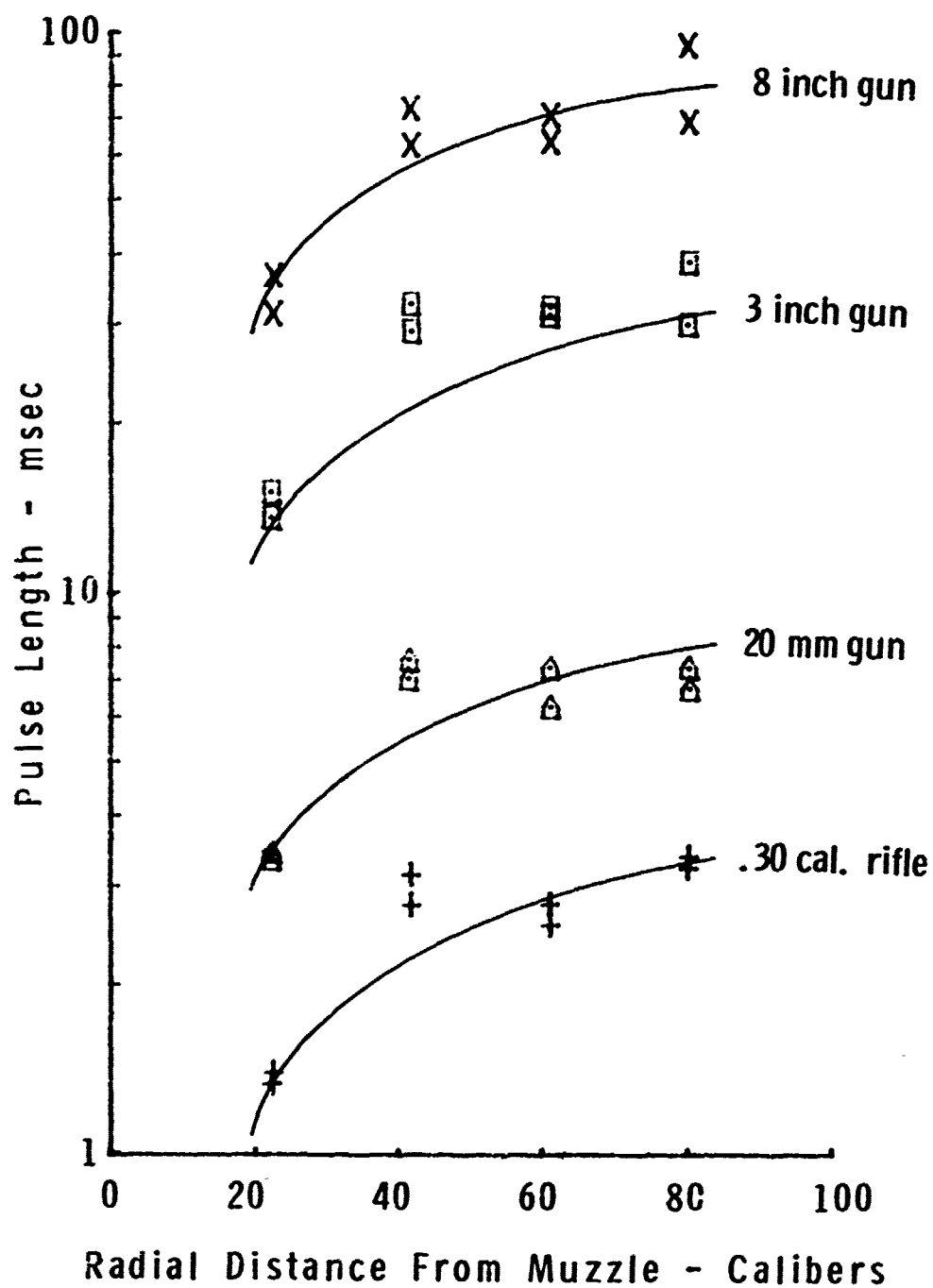


FIGURE 12. Overpressure Pulse Length for Four Guns.

APPENDIX A

The form of the geometry function $G(\theta)$ was developed on the basis of a moving charge. If the velocity at some point in the blast field is the sum of the charge velocity \vec{V}_c and the blast velocity for a stationary charge \vec{V}_s then $\vec{V} = \vec{V}_c + \vec{V}_s$ is assumed to be in the direction of the radius vector from the muzzle. If the field position is determined by the distance from the muzzle and the polar angle relative to the line-of-fire then θ is the angle between \vec{V} and \vec{V}_c and

$$V_s^2 = V^2 + V_c^2 - 2VV_c \cos \theta \quad A1$$

or

$$\left(\frac{V}{V_s}\right)^2 - 2\frac{V}{V_s} \frac{V_c}{V_s} \cos \theta + \left(\frac{V_c}{V_s}\right)^2 - 1 = 0 \quad A2$$

Solving for the ratio V/V_s we obtain

$$\frac{V}{V_s} = \frac{V_c}{V_s} \left\{ \cos \theta \pm \sqrt{\cos^2 \theta - \left[1 - \left(\frac{V_s}{V_c}\right)^2 \right]} \right\} \quad A3$$

We assume that the geometry factor has a similar form ie.

$$G(\theta) = \alpha \left(\cos \theta + \sqrt{\cos^2 \theta + \beta^2} \right) \quad A4$$

where α and β are constants to be determined.

If we require that at the angle $\theta = \pi/2$ the geometry factor have the value unity then

$$\beta = 1/\alpha \quad A5$$

Henricksen and Cummings² find that the kinetic energy of ordered motion at the muzzle is approximately twice that of random motion. Based on this result we require

$$G(0) = 2 \quad A6$$

This gives the results

$$\alpha = 3/4 \quad A7$$

and

$$G(\theta) = \frac{3}{4} \left[\cos \theta + \sqrt{\cos^2 \theta + \frac{4}{3}} \right] \quad A8$$

APPENDIX B

A BASIC computer program has been constructed to perform the calculations for the muzzle blast field based on the preceding analysis. The program is listed at the end of this appendix. The input parameters required for the program are as follows:

1. Projectile mass - kilograms (kg)
2. Muzzle velocity - metres/second (m/s)
3. Propellant specific energy - joules/kilogram (J/kg)
4. Ratio of peak chamber pressure to atmospheric pressure - dimensionless
5. Barrel length - metres (m)
6. Barrel diameter - metres (m)
7. Height of the barrel rifling - metres (m)

When execution of the program begins the program will pause for input until these values are entered in the order given above. When the last value is entered the program calculates the overpressure at the choke position and at the muzzle and an equivalent explosive yield. Next, the program will pause to allow optional values of Q1, Q2 and ratio of specific heats, γ to be entered if desired. The variables Q1 and Q2 are the exponents in the Porzel QZQ hypothesis for the strong and weak shock regimes and have the standard values 3.25 and 3.5 respectively. The standard value of γ is 1.4. After the option is exercised the program computes the transition radius and pauses until the desired angular position in the blast field is entered. This is the angle θ measured from the line of fire to the radius vector from the muzzle to the field location and lies between 0° and 180° .

The program is designed to calculate overpressure and pulse length as a function of distance from the muzzle at the input angle θ . The program will pause until the desired distance closest to the muzzle is entered. It then pauses until an increment in the radial distance is entered and again until the total number of increments desired is entered. The program then computes the overpressure and pulse lengths at each radial location specified for the angle θ specified. When these computations are completed the program pauses to allow the option of terminating the program or specifying another angle θ . If a new angle is entered then the program pauses to allow an option of continuing with the same radial locations or changing to new radial locations. When the last angular position desired has been calculated the operator enters minus one (-1) to terminate execution.

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00000 100 FOR N=1 TO 5 STEP 1
00001 116 PRINT
00002 120 NEXT N
00003 140 PRINT "MUZZLE BLAST OVERPRESSURE AND PULSE LENGTH"
00004 150 PRINT "-----"
00005 160 PRINT
00006 170 PRINT
00007 200 REM . . INPUT SECTION . . : ARE AS FOLLOWS:
00008 201 REM . . VARIABLE DEFINITIONS ARE AS FOLLOWS:
00009 202 REM . . PROJECTILE: V0 - VELOCITY (M/SEC), W0 - MASS (KG)
00010 205 REM . . PROPELLANT: W1 - MASS (KG), X1 - SP. GRAVITY (KG/M**3)
00011 206 REM . . SPECIFIC ENERGY (J/KG)
00012 207 REM . . PRESSURE: P - CHAMBER PRESSURE RATIO (P/P0)
00013 208 REM . . BARREL: L0 - LENGTH ("), D0 - DIAMETER ("),
00014 209 REM . . LI - GROOVE HEIGHT (RIFLING) (M)
00015 210 PRINT "PROJECTILE", "MASS (KG)", ,
00016 211 INPUT W0
00017 225 PRINT "VELOCITY (M/SEC)",
00018 230 INPUT V0
00019 240 PRINT
00020 245 PRINT
00021 246 PRINT "PROPELLANT", "MASS (KG)", ,
00022 250 PRINT
00023 260 INPUT W1
00024 265 PRINT
00025 265 PRINT "SPECIFIC ENERGY (J/KG)",
00026 290 PRINT, X2
00027 300 INPUT X2
00028 305 PRINT
00029 306 PRINT "CHAMBER PRESSURE RATIO (P/P0)", ,
00030 310 PRINT
00031 320 INPUT P0
00032 325 PRINT
00033 326 PRINT

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0034 500 PRINT "BARREL", "LENGTH (")",,
0035 540 INPUT L0
0036 545 PRINT
0037 550 PRINT "DIAMETER (")",,
0038 560 INPUT D0
0039 565 PRINT
0040 570 PRINT "GROOVE HEIGHT (")",
0041 580 INPUT L1
0042 590 PRINT
0043 595 PRINT
0044 600 REM . . . END INPUT DATA
0045 1000 REM . . .
0046 1010 REM . . . BEGIN ENERGY CALCULATIONS
0047 1011 REM . . . E(POP)=E2, E(PROJ)+E1, E(AVAIL)=E3
0048 1020 LET E2=X2*.11
0049 1030 LET E1=.5*.10*V0**2
0050 1040 LET E3=E2-E1
0051 1050 PRINT
0052 1060 PRINT " " ENERGY CALCULATIONS"
0053 1070 PRINT
0054 1080 PRINT "TOTAL ENERGY IN PROPELLANT",E2;"JOULES"
0055 1090 PRINT "KINETIC ENERGY IN PROJECTILE",E1;"JOULES"
0056 1100 PRINT "MAXIMUM AVAILABLE ENERGY",E3;"JOULES"
0057 1110 LET PJ=P0-1
0058 2000 PRINT
0059 2001 PRINT " " INTERIOR LOSSES"
0060 2002 PRINT
0061 2010 REM . . . ROUGHNESS FACTOR=H, OVERPRESSURE RATIO AT CHOKE=Y
0062 2020 REM . . . O'PRESSURE RATIO AT MUZZLE AND INITIAL YIELD=Y0
0063 2021 REM . . . CHOKE LENGTH=L2
0064 2030 LET H=L1/DJ
0065 2040 LET L2=0
0066 2050 LET X=P0
0067 2060 REM . . . IF CHOKE LENGTH L/D ASSUME NO CHARGE LOSSES
0068 2065 IF H=J GOTO 2100
0069 2070

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0069 2070 IF L5/H**1>(L0/70)GOTO 2100
0070 2071 LET L2=L5/H**1
0071 2072 REM .: IF P0>100 USE FITTED CURVE
0072 2100 IF P0>100 GOTO 2100
0073 2110 LET X=P0
0074 2120 LET C=(1+X)*(1+4*X**2/5/(1+X))/(1+X)**5-1
0075 2130 IF ABS (C-P0)<.001 GOTO 2170
0076 2140 LET X=X-(X-1)*(C-P0)/(C-1.29)
0077 2150 GOTO 2110
0078 2160 LET X=EXP (.9211*LOG (P0)-2.137)
0079 2170 PRINT "OVERPRESSURE RATIO AT";L2*P0;" IS",X;" (CHOKER)"
0080 2180 LET Y0=EXP((2*H*(L2-L0/P0)+1.063*LOG (X))/1.07)
0081 2190 PRINT "OVERPRESSURE AT";L0;" IS",Y0;" "HEZLE"
0082 2200 LET F=P0/Y0
0083 2210 REM .: REDUCTION IS AVAILABLE
0084 2220 LET Y0=E0/(G*F)
0085 2230 LET E3 = W1/12*V0**2
0086 2240 LET Y0=Y0+E3
0087 2250 PRINT
0088 2260 PRINT , " EQUIVALENT EXPLOSION PARAMETERS"
0089 2270 PRINT
0090 2280 PRINT "YIELD",Y0;" JOULES"
0091 2290 LET R0=D0
0092 2300 LET M0=W1/6
0093 2310 FOR M=1 TO 5 STEP 1
0094 2320 PRINT
0095 2330 NEXT M
0096 2340 PRINT "FOR OPTIONAL Q1,Q2,GAMMA ENTER ONE; STANDARD VALUES ENTER ZERO"
0097 2350 INPUT Q1
0098 2360 IF Q1=0 GOTO 2370
0099 2370 PRINT "ENTER Q1"
0100 2380 INPUT Q1
0101 2390 PRINT "ENTER Q2"
0102 2400 PRINT
0103 2410 PROCEED

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0102 2275 INPUT Q2
0103 2276 PRINT "ENTER RATIO OF SPECIFIC HEATS, GAMMA"
0104 2277 INPUT G
0105 2278 GOTO 2300
0106 2279 LET Q1=3.25
0107 2280 LET Q2=3.5
0108 2281 LET G=1.4
0109 2282 REM ..Q1=PRESSURE/DENSITY(ATMOSPHERIC)
0110 2283 LET Q0=76340
0111 2284 LET H=.25
0112 2285 LET Q5=1889
0113 2286 LET P0=101525
0114 2287 LET D=1.293
0115 2288 LET M=M0*H/5.416
0116 2289 LET Z0=(R0*.5+H)**(1/3)
0117 2290 REM ..FIND TRANSITION RADIUS
0118 2291 LET A1=(Q1-Q2)/(3-Q2)
0119 2292 LET A2=(Q1-3)*Y0/(12.566*.05*Z0**3)
0120 2293 IF Q1=Q2 GOTO 2430
0121 2294 LET Z=1
0122 2295 LET S=Z
0123 2296 LET F=A1*S**3-S**Q1+A2
0124 2297 LET F1=3*A1*S**2-Q1*S**(Q1-1)
0125 2298 LET Z=Z-F/F1
0126 2299 IF ABS(Z-S)<.001 GOTO 2430
0127 2300 GOTO 2451
0128 2301 LET Z1=Z
0129 2302 GOTO 2481
0130 2303 LET Z1=A2**((1/Q1))
0131 2304 LET R2=((Z1*Z0)**3-H)**(1/3)
0132 2305 PRINT "TRANSITION RADIUS",R2,"METERS"
0133 2306 REM ..SET UP QZQ CONSTANTS A AND B
0134 2307 LET A=Q5/Q0*(Z1**Q1)
0135 2308 LET B=Q5/Q0*Z1**Q2
0136 2309 PROCEED

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0136 2030 PRINT
0137 2040 PRINT
0138 2050 REM ** GET UP DECLER RADIAL LOCATIONS
0139 2060 PRINT "INPUT ANGLE "I"(DEGREES)"
0140 2070 INPUT I
0141 2080 LET T2=COS(T1*3.14159/. )
0142 2090 LET R2=.7*(T2+COS(V2*T2+. ))
0143 2100 PRINT "ENTER INITIAL RADIAL LOCATIONS"
0144 2110 INPUT R3
0145 2120 PRINT "INPUT RADIAL LOCATIONS "I"(DEGREES)"
0146 2130 INPUT R4
0147 2140 PRINT "INPUT NUMBER OF INCREMENTS BETWEEN"
0148 2150 INPUT K
0149 2160 PRINT "RADIALS", "OVERPERCENTAGE", "NUMBER OF INCREMENTS"
0150 2170 PRINT " (PERCENTS)", " (P-P)", "P/P", " (PERCENTS)"
0151 2180 PRINT "*****", "*****", "*****"
0152 2190 LET C1=0
0153 2200 LET C2=COS(C*PI/D)
0154 2210 LET T3=R2*R3/100
0155 2220 FOR I=1 TO K STEP 1
0156 2230 LET R=(R3+R4*(I-1))
0157 2240 FOR J=1 TO 10 STEP 1
0158 2250 IF R<R2*R3 GOTO 2700
0159 2260 IF (R-R2*R3)<R4 GOTO 2700
0160 2270 LET Y2=R4/10
0161 2280 GOTO 2710
0162 2290 LET Y2=(R-R2*R3)/1
0163 2300 LET Y=(R-(10-J)*Y2)/R3
0164 2310 COSUR 4000
0165 2320 LET U=(P1-1)+COS(2*PI/(C+1)*PI+(C-1))
0166 2330 LET C1=C1+Y2/(1+(C+1)/. )*(U/C)
0167 2340 NEXT J
0168 2350 LET T=T3+(R-R2*R3)-C1/C
0169 2360 GOTO 2710
0170 2370 PRINT
0171 2380

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0170 2780 LET T=T5
0171 2785 LET V=R/R8
0172 2790 GOSUB 4000
0173 2800 LET P=PI-1
0174 2810 PRINT R,P,T
0175 2820 GOTO 2840
0176 2830 PRINT "ERROR;RADIUS",R,"LESS THAN MUZZLE DIAMETER"
0177 2840 NEXT I
0178 3040 PRINT "INPUT NEXT ANGLE(DEGREES) OR NEG ONE TO TERMINATE"
0179 3041 INPUT T1
0180 3050 IF T1<0 GOTO 3070
0181 3051 LET T2=COS(T1*.14159/180)
0182 3052 LET R8=.75*(T2+SQR(T2*T2+16/9))
0183 3060 PRINT "ENTER ONE TO CHANGE RADIUS;ENTER ZERO TO CONTINUE"
0184 3061 INPUT A8
0185 3062 IF A8=0 GOTO 2025
0186 3063 GOTO 2006
0187 3070 PRINT "END OF UTE MUZZLE BLAST CALCULATIONS"
0188 3080 GOTO 9999
0189 4000 IF V<=R0 GOTO 2330
0190 4010 LET Z=((V**3+M)**(1/3))/Z0
0191 4020 IF Z<= Z1 GOTO 4060
0192 4030 LET Q=B/(Z**Q2)
0193 4040 LET Y1=Q0*Q/(Q2-3)*(Z0*Z)**3
0194 4050 GOTO 4070
0195 4060 LET Q=A/(Z**Q1)
0196 4070 REM ..NOW CALCULATE OVERPRESSURE
0197 4080 IF Q<7.45E-7 GOTO 4210
0198 4090 IF Q>1.167 GOTO 4310
0199 4100 LET P1=5
0200 4110 LET A1 = (G+1)/(G-1)+P1
0201 4120 LET A2 = (G+1)/(G-1)*P1+1
0202 4130 LET A3 = 1+(G-1)*Q
0203 4140 LET F =A1*P1*(1/G)-A3*A2
PROCEED

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```
0204 4150 LET F1 = 1/G*A1*P1**((1/G-1)+P1**((1/G)
0205 4160 LET F1 = F1-(G+1)/(G-1)*A3
0206 4170 LET N=F/F1
0207 4180 IF ABS(N)<.001 GOTO 4340
0208 4190 LET P1=P1-N
0209 4200 GOTO 4110
0210 4210 LET P=.02
0211 4220 LET C1=24*Q*G**3/(G+1)
0212 4230 LET F=3*P**4-2*P**3+C1
0213 4240 LET F1=12*P**3-G*P**2
0214 4250 LET N=F/F1
0215 4260 IF ABS(N)<.0005 GOTO 4290
0216 4270 P=P-N
0217 4280 GOTO 4230
0218 4290 P1=P+1
0219 4300 GOTO 4340
0220 4310 LET K1=22+16*LOG(Q)/2.303
0221 4320 LET L=11.5-SQR(132.25-K1)
0222 4330 LET P1=10**L+1
0223 4340 RETURN
0224 9999 END
END OF WORK FILE
```